The RDF language

Department of Computer Science Universidad de Chile

> Center for Web Research http://www.cwr.cl

UPM, Madrid 2009



RDF Semantics

W3C Recommendation 10 February 2004

This Version:

http://www.w3.org/TR/2004/REC-rdf-mt-20040210/

http://www.w3.org/TR/rdf-mt/

http://www.w3.org/TR/rdf-mi

http://www.w3.org/TR/2003/PR-rdf-mt-20031215/

Editor:

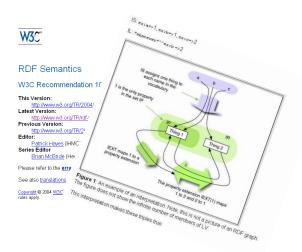
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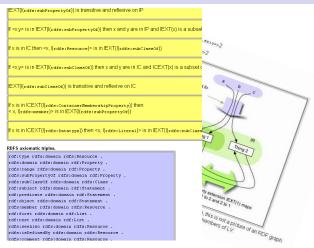
Brian McBride (Hewlett Packard Labs)
bwm@hplb.hpl.hp.com>

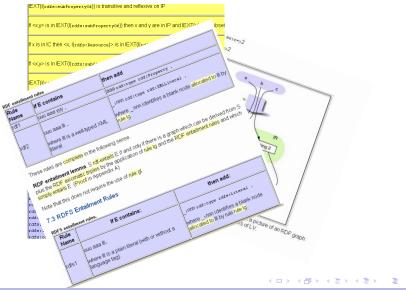
Please refer to the errata for this document, which may include some norn

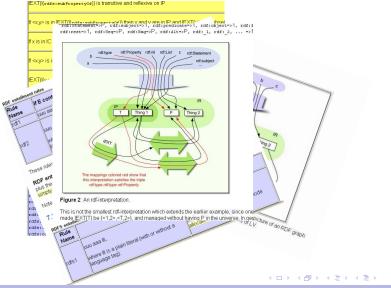
See also translations

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Several dozens of reserved keywords...

```
rdfs:Resource [res]
rdf:Property [prop]
rdfs:Class [class]
rdfs:Literal [literal]
rdfs:Datatype [datatype]
rdf:XMLLiteral [xmlLit]
rdfs:Container [cont]
rdf:Statement [stat]
rdf:List [list]
rdf:Alt [alt]
rdf:Bag [bag]
rdf:Seg [seg]
```

```
rdf:type [type]
                                rdfs:domain [dom]
                                rdfs:range [range]
                                rdfs:subClassOf [sc]
                                rdfs:subPropertyOf [sp]
                                rdf:subject [subj]
                                rdf:predicate [pred]
                                rdf:object [obj]
                                rdfs:member [member]
                                rdf:first [first]
                                rdf:rest [rest]
                                rdfs:seeAlso [seeAlso]
rdfs:ContainerMembershipProperty [contMP]
```

```
rdfs:isDefinedBy [isDefined]
rdfs:comment [comment]
rdfs:label [label]
rdf:value [value]
rdf:nil [nil]
rdf:_1 [_1]
rdf:_2 [_2]
rdf:_i [_i]
```

...plus axiomatic triples...

```
prop)
(type,
           type,
(subj,
                         prop)
           type,
(pred,
           type,
                         prop)
(obj,
           type,
                         prop)
(first,
                         prop)
           type,
(rest,
                         prop)
           type,
(value,
           type,
                         prop)
_1,
                         prop)
           type,
(_1,
                      contMP)
           type,
           type,
                         prop)
           type,
                      contMP)
(_i,
           type,
                         prop)
(_i,
                      contMP)
           type,
(nil,
                         prop)
           type,
(xmlLit,
           type,
                    datatype)
```

...plus more axiomatic triples...

```
res)
                                                                   class)
(type,
                dom.
                                      (type,
                                                      range,
                                                                   class)
(dom,
                dom,
                         prop)
                                      dom,
                                                      range,
                                                                   class)
(range,
                dom,
                         prop)
                                      (range,
                                                      range,
(sp,
                dom.
                         prop)
                                      (sp,
                                                                    prop)
                                                      range,
                        class)
                                                                   class)
(sc.
                dom,
                                      (sc.
                                                      range,
(subj,
                dom.
                         stat)
                                      (subj,
                                                                     res
                                                      range,
(pred.
                dom,
                         stat)
                                      (pred,
                                                      range,
                                                                     res)
(obj.
                dom.
                         stat)
                                      (obj.
                                                      range,
                                                                     res)
(member.
                dom.
                          res)
                                       member.
                                                      range,
                                                                     res)
(first,
                         list)
                                      (first,
                dom,
                                                      range,
                                                                     res)
(rest,
                dom.
                         list)
                                      rest.
                                                      range,
                                                                    list)
(seeAlso,
                dom.
                          res)
                                      (seeAlso,
                                                      range,
                                                                     res)
(isDefined,
                dom,
                          res)
                                      (isDefined,
                                                      range,
                                                                     res)
comment.
                dom,
                          res)
                                       comment.
                                                      range,
                                                                literal)
(label,
                dom,
                          res)
                                      (label,
                                                      range,
                                                                literal)
(value,
                dom,
                                      (value,
                          res)
                                                      range,
                                                                     res)
(_1,
                dom.
                          res)
                                      (_1,
                                                      range,
                                                                     res)
(_2,
                          res)
                                      (_2,
                dom,
                                                      range,
                                                                     res)
(_i,
                                      (_i,
                dom.
                          res)
                                                      range,
                                                                     res)
. . .
                                      . . .
```

...plus more axiomatic triples...

```
(alt,
       sc.
                cont)
(bag,
        sc,
                 cont)
(seq, sc,
                 cont)
(contMP, sc, prop)
(xmlLit, sc,
              literal)
(datatype,
                class)
         sc,
(isDefined, sp,
               seeAlso)
```

...and on top of this a (slightly) non-standard model theory

► A notion of interpretation

including subsets of the universe denoting properties, classes and literals, and mapping defining their extensions.

- Notion of interpretation of blank nodes
- Definition of reflexivity, transitivity and semi-extensionality of subClass and subProperty
- Typing restrictions

But...we need a workable language to bring to reality the vision of the Semantic Web

Would like to:

- ► Have a simple user-language to be able to popularize RDF among Web users.
- ► Have a simple specification to allow sound development work.
- ► Have a language in streamlined form to make it easy to formalize and prove results about its properties.

What is to be done?: To simplify the language

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There is a minimal fragment of the theory preserving the essential core of RDFS

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There is a minimal fragment of the theory preserving the essential core of RDFS

- ▶ Basic idea: Separate user-language from features and constructors which define and specificy the language.
- Concentrate in vocabulary with non-trivial semantics.

Main contributions & Outline

- Identify a fragment of RDFS that covers the crucial vocabulary and preserves the original RDFS semantics.
- Study dependencies among vocabulary and develop sound and complete proof systems for each fragment.
- Present algorithms to modularize reasoning according to relevant vocabulary.

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The core vocabulary

rdfs:Resource [res] rdf:Property [prop] rdfs:Class [class] rdfs:Literal [literal] rdfs:Datatype [datatype] rdf:XMLLiteral [xmlLit] rdfs:Container [cont] rdf:Statement [stat] rdf:List [list] rdf:Alt [alt] rdf:Bag [bag] rdf:Seg [seg]

rdf:type [type] rdfs:domain [dom] rdfs:range [range] rdfs:subClassOf [sc] rdfs:subPropertyOf [sp] rdf:subject [subj] rdf:predicate [pred] rdf:object [obj] rdfs:member [member] rdf:first [first] rdf:rest [rest] rdfs:seeAlso [seeAlso] rdfs:ContainerMembershipProperty [contMP]

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```

```
\rho df = \{ sp, sc, type, dom, range \}
```

Blank node rule

 $rac{G}{H}$ if there is a homomorphism $\mu: H o G$

Subproperty (transitivity, definition)

$$\frac{(A,\operatorname{sp},B) (B,\operatorname{sp},C)}{(A,\operatorname{sp},C)}$$

$$\frac{(A,\operatorname{sp},B)(X,A,Y)}{(X,B,Y)}$$

Subclass (transitivity, definition)

$$\frac{(A, \operatorname{sc}, B) (B, \operatorname{sc}, C)}{(A, \operatorname{sc}, C)}$$

$$\frac{(A, \text{sc}, B) \ (X, \text{type}, A)}{(X, \text{type}, B)}$$

Typing (domain, range)

$$\frac{(A, \text{dom}, B) (X, A, Y)}{(X, \text{type}, B)}$$

$$\frac{(A, range, B) (X, A, Y)}{(Y, type, B)}$$

$$\frac{(A,\mathtt{dom},B)\ (C,\mathtt{sp},A)\ (X,C,Y)}{(X,\mathtt{type},B)}$$

$$\frac{(A, \mathtt{range}, B) \ (C, \mathtt{sp}, A) \ (X, C, Y)}{(Y, \mathtt{type}, B)}$$

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$$\frac{(A, sc, B) (B, sc, C)}{(A, sc, C)}$$

$$\frac{(A, \text{sc}, B) \ (X, \text{type}, A)}{(X, \text{type}, B)}$$

Typing (domain, range)

$$\frac{(A, dom, B) (X, A, Y)}{(X, type, B)}$$

$$\frac{(A, \mathtt{range}, B) \ (X, A, Y)}{(Y, \mathtt{type}, B)}$$

$$\frac{(A, \text{dom}, B) \ (C, \text{sp}, A) \ (X, C, Y)}{(X, \text{type}, B)}$$

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Reflexivity rules

If "
$$(A, type, Property)$$
" then (A, sp, A)

Subproperty Reflexivity

$$\frac{(X,A,Y)}{(A,\operatorname{sp},A)} \qquad \qquad \frac{(p,\operatorname{sp},p)}{(p,\operatorname{sp},p)} \text{ for } p \in \rho \operatorname{df}$$

$$\frac{(A,\operatorname{sp},B)}{(A,\operatorname{sp},A)} \qquad \frac{(A,\operatorname{dom},X)}{(A,\operatorname{sp},A)} \qquad \frac{(A,\operatorname{range},X)}{(A,\operatorname{sp},A)}$$

Subclass Reflexivity

$$\frac{(A, \operatorname{sc}, B)}{(A, \operatorname{sc}, A) (B, \operatorname{sc}, B)} \qquad \frac{(X, \operatorname{range}, A)}{(A, \operatorname{sc}, A)}$$

$$\frac{(X, \operatorname{dom}, A)}{(A, \operatorname{sc}, A)} \qquad \frac{(X, \operatorname{type}, A)}{(A, \operatorname{sc}, A)}$$

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$$\frac{(X, \operatorname{dom}, A)}{(A, \operatorname{sc}, A)} \qquad \frac{(X, \operatorname{type}, A)}{(A, \operatorname{sc}, A)}$$

Soundness and Completeness

Let \models denote the standard RDFS entailment, and $\vdash_{\rho df}$ a proof system based on the rules presented.

Theorem

Let G and H be graphs in ρ df then

$$G \models H$$
 if and only if $G \vdash_{\rho df} H$.

Blank Nodes Modularization

Blank nodes can be treated in an orthogonal form to ρdf vocabulary.

Theorem

Let G and H be graphs in ρ df and $G \models H$, then

there is a proof of H from G where the blank rule is used at most once and at the end.

The role of reflexivity

The only consequence of reflexivity of sp and sc in RDFS is the possible entailment of triples of the form (x, sp, x), (x, sc, x).

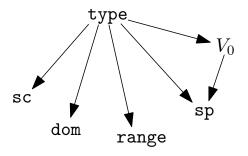
Theorem

Let G and H be ρ df graphs. Assume that H does not contain triples of the form (x, sp, x) and (x, sc, x). Then,

 $G \vdash_{\rho df} H$ without using reflexivity rules.

(Also, by not imposing reflexivity, axiomatic triples can be completely avoided.)

Dependence diagram among ρ df vocabulary



To determine $G \models H$ it is enough to test $G' \models H$ where G' is the subgraph of G which involves only nodes in voc(H) and their dependencies in the diagram.

It is possible to avoid the closure to test RDFS entailment

- ▶ A naive approach to test $G \models H$ is:
 - ▶ (pre-)compute the closure of *G*
 - check if H is contained in the closure of G.

Theorem

The size of the closure of G is $O(|G|^2)$, and this bound is tight.

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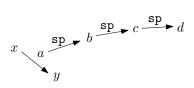
Theorem

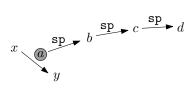
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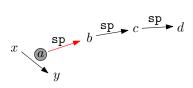
► Alternative: to use a goal oriented approach based on the dependencies diagram.

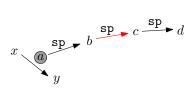
Goal oriented entailment algorithm

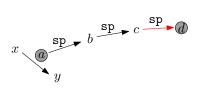
Does the graph entails (x, d, y)? Look for triples of the form (x, a, y) and sp-paths from a to d.

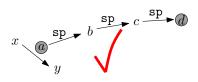


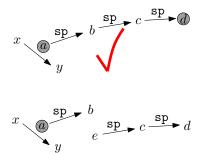


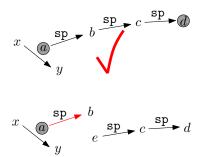


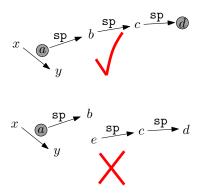


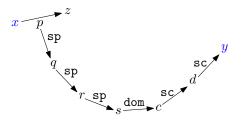


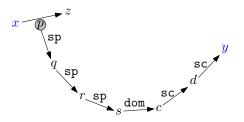


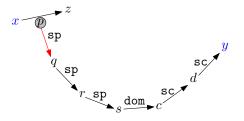


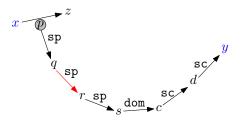


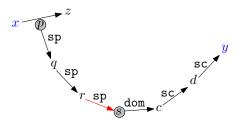


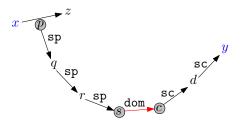


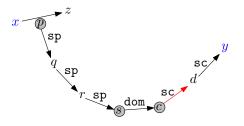


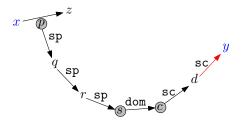


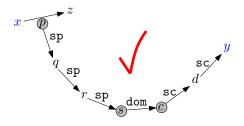












Entailment can be done in $O(n \log n)$ time

Theorem

The goal oriented algorithm takes $O(|G| \log |G|)$ time in testing the entailment $G \models t$.

- ▶ Correctness follows by the dependencies diagram.
- ▶ Essentially time $|G| \log |G|$ in constructing the necessary graph data-structures.
- ▶ Time |G| in traversing these data-structures.

There is no more efficient approach to test $G \models t$!

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The $O(n \log n)$ bound is tight.

Theorem

Testing $G \models t$ takes time $\Omega(|G| \log |G|)$.

Idea: Coding the set-disjointness problem, which is $\Omega(n \log n)$

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- ▶ Efficient algorithm to check entailment

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- Next: Navigational language based on testing algorithm