

## Queries and Computation on the Web

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- » The web: tremendous source of information.
- » Can be viewed as a large, loosely structured database .
- » So can we query it like a database?. First we need:
  - > A model of the web.
  - A suitable query language.
- » Which queries are actually computable?

### Introduction

- » Infinite web : exhaustive exploration is unfeasible.
- » It is an infinite set of **objects** which have a **value** and **labeled references** to other object. e2

e1

2

e3

3

e4

INTUITION:
 Objects are web pages.

>>

References are links.

### The Model

#### » Formaly – An infinite database over the fixed relational schema:

#### 

- $Obj = \pi_{source}(Ref) \cup \pi_{oid}(Val)$
- $\pi_{dest}(Ref) \subseteq Obj$

- $\forall o \in Obj \ \sigma_{source=o}(Ref)$  is finite.
- At most one value per object.

### The model

- » We want to compute queries over web instances.
- » Queries are **mappings** from a web instances I to a subset of I(Obj).
- » Generic query: q is generic if for each web instance / and one-to-one mapping ρ : q(ρ(l))=ρ(q(l))
- » INTUITON : The result only depends on the information of I and does not depend on the encoding.

Computability

#### » Web Machine : Like a Turing Machine but with...

- <sup>></sup> A right-infinite input tape.
- <sup>></sup> A two-way-infinite work tape.
- <sup>></sup> A right-infinite output tape.
- » Initial State : input tape contains an encoding of the Web Instance.
- » Output head can only move forward (nothing is deleted).



- » Computability requires an initial set of known objects.
- » Computable: There exists a WM which on input enc(I) halts and produces enc(q(I)).
- » Eventually Computable: Exists a WM for which
  - > The content of the output tape is always a prefix of enc(q(I))
  - \* Each o in q(I) occurs <u>at some point</u> in the computation.



- » Computable
  - Find the objects o' such that there is a path of length at most k from o to o'.
- » Eventually Computable, possibly infinite answers
  - Find the objects reachable from o.
- » Eventually Computable, finite answers
  - Find the objects on the shortest cycle containing o.
- » Not eventually computable
  - <sup>></sup> Find all objects which are not referenced by any object.



- » In practice we use two modes of computation: Browsing and Searching.
- » Browse Machine, like a Web Machine but with an *expand* state and a browse tape instead of input tape.
- » Initially, the browse tape contains the encoding of an initial object **o**.
- » **Expands** replaces the browsing tape with the encoding of all nodes referenced in it.

### Browse & Search >

#### "Every generic and computable Web Query is browser computable."

### Browse & Search

#### » Browse/Search Machine, a Browse Machine with

- » A search-answer tape.
- » A search-condition tape.
- » Conditions involve a finite set of (in)equalities involving an attribute and a constant.

 $\sigma_{value=uchile}(Val)$ :

"Search for all tuples Val(o, 'uchile')"



"A generic Web query is eventually computable iff it is eventually computable by a browse/search machine."

"A generic Web query is computable iff it is computable by a browse/search machine"

### Browse & Search >

» We consider FO (First-order logic), FO+ (without negation), Datalog and Datalog¬ (with negation).

- » Are the queries on each language (eventually) computable?
- » Which fragment of each language can be implemented by browsers?

#### "All FO+ and Datalog queries are eventually computable."



#### » Source-ranged-restricted variables

- If R(u) occurs in the body of the rule, R is some idb predicate and x is one of the variables of u, then x is source-range-restricted.
- If x is the source constant or x is source-rangerestricted and Ref(x,y,z) appears in the body of the rule, then y and z are source-rangerestricted.
- If x is the source constant or x is source-rangerestricted and Val(x,y) occurs in the body, y is source-range-restricted.

» Source safe: answer(source) ← answer('t) ← answer(t), Ref(t,x,t')

» Not source safe: answer(source) ← answer('t) ← answer(t'), Ref(t,x,t')

"All ss-FO queries are computable by a browser machine."

"All ss-Datalog queries are eventually computable by a browser machine."



### » Datalog ¬, problems arise with negation:

- $P \leftarrow \neg P$
- Single(x)  $\leftarrow$  Man(x),  $\neg$  Married(x)
- <sup>></sup> Married(x) ← Man(x), ¬ Single(x)

#### » Has different semantics

- Well-founded semantics
- Stratified semantics
- Inflationary semantics

"Every query in ss-Datalog with inflationary semantics is eventually computable by a browser machine."

#### **Conclusion** :

# ss-Datalog vith inflationary semantics emerges as a particularly appealing language in the context of the web.